

☺ Chapter 4 Notes ☺

4.2 – Function Notation

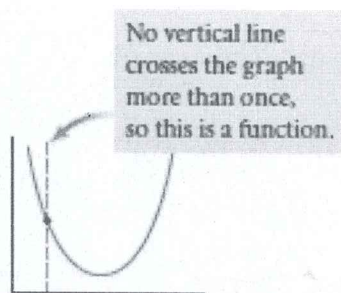
Daily Objective:

1. Define function
2. Review function notation
3. Review the vertical line test for functions
4. Distinguish between functions and relations
5. Define domain and range of a function

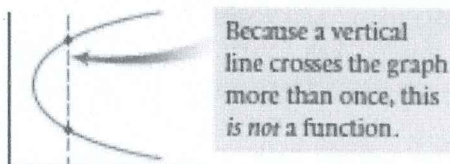
Relation: *any relationship between variables*

Function: *a special type of a relation where each independent variable (x), is assigned exactly one dependent variable (y).*

Each x has exactly one y.



Function



Not a function

Function Notation: $y = f(x)$ "f of x" y is a function of x
x goes into the rule/equation f and y comes out

***** $f(x)$ does not mean f times x *****

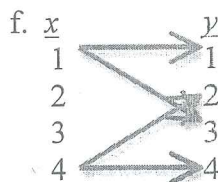
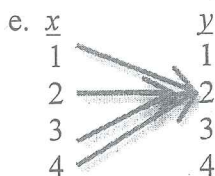
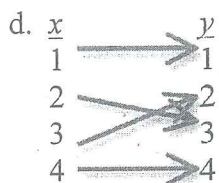
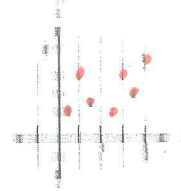
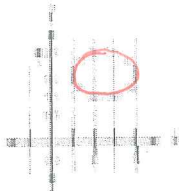
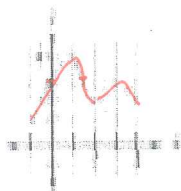
**** You do not have to use the letter f for function notation, you may pick another letter ****

Does the definition of function require that there be only one value of x for each value of y ?

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Investigation To Be or Not to Be (a Function)

REPLY TO THE QUESTIONS ON THE INVESTIGATION.



- g. Independent variable: the age of each student in your class
Dependent variable: the height of each student
- h. Independent variable: an automobile in the state of Kentucky
Dependent variable: that automobile's license plate number
- I Independent variable: the day of the year
Dependent variable: the time of sunset

Step 1: Identify each relation that is also a function. For each relation that is not a function, explain why not.

a) *FUNCTION*

b) *NOT A FUNCTION - THERE ARE X-VALUES WITH MORE THAN 1 Y-VALUES*

c) *FUNCTION*

d) *FUNCTION*

e) *FUNCTION*

f) *NOT A FUNCTION*
1 IS PAIRED WITH 2 Y (1, 3)
4 IS PAIRED WITH 2 Y (2, 4)

g) *NOT A FUNCTION*

STUDENTS MIGHT HAVE SAME AGE BUT DIFF HEIGHT

16 → 6'0"
16 → 6'2"

h) *FUNCTION*

EACH AUTO HAS OWN #

i) *IF ONE YEAR ONE LOCATION: FUNCTION*
IF MULTIPLE YEARS: NOT A FUNCTION
IF MULTIPLE LOCATIONS: NOT A FUNCTION

Step 2: For each graph or table that represents a function, find the y-value when $x = 2$, and find the x-value(s) when $y = 3$. Write each answer in function notation.

a) $f(2) = 2$

$f(0) = 3$
and
 $f(1.5) = 3$

c) $f(2)$ is undefined

$f(1) = 3$ and
 $f(3) = 3$

d) $f(2) = 3$

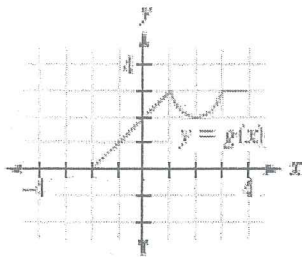
$f(2) = 3$

e) $f(2) = 2$

no x-value results
in $y = 3$

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Example 1: Function g is defined by the graph below:



Find these values:

$$g(-2) = \underline{0} \quad g(0) = \underline{2} \quad g(1) = \underline{3} \quad g(4) = \underline{2}$$

Find x when $g(x) = 0$. -2

What is the range?

$$0 \leq g(x) \leq 3$$

What is the domain?

$$-2 \leq x \leq 4$$

Example 2: Given $f(x) = 2x - 4$, find the values below:

a. $f(1) = 2(1) - 4$

$$= 2 - 4$$

$$\boxed{f(1) = -2}$$

b. $f(9) = 2(9) - 4$

$$= 18 - 4$$

$$\boxed{f(9) = 14}$$

c. $f(-3) = 2(-3) - 4$

$$= -6 - 4$$

$$\boxed{f(-3) = -10}$$

Example 3: Given $h(x) = \frac{2x+5}{x-3}$, find the values below:

a. $h(8) = \frac{2(8)+5}{8-3}$

$$= \frac{16+5}{5}$$

$$= \frac{21}{5}$$

$$\boxed{h(8) = 4\frac{1}{5}}$$

b. $h(-7) = \frac{2(-7)+5}{-7-3}$

$$= \frac{-14+5}{-10}$$

$$= \frac{-9}{-10}$$

$$\boxed{h(-7) = \frac{9}{10}}$$

c. $h(15) = \frac{2(15)+5}{15-3}$

$$= \frac{30+5}{12}$$

$$= \frac{35}{12}$$

$$\boxed{h(15) = 2\frac{11}{12}}$$